

Start here for
Question Number: **2**

$$a) \quad \frac{\cos x}{x}$$

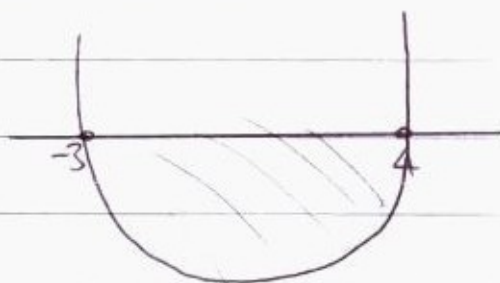
+ 5
+ 0
- 5
- 0
+ 5

$$\frac{d}{dx} = \frac{(x \sin x) - \cos x}{x^2}$$

$$b) \quad x^2 - x - 12 < 0$$

$$\therefore x = \frac{-4}{3}$$

$$(x-4)(x+3) < 0$$



$$\therefore -3 < x < 4$$

$$c) \quad y = \ln(3x)$$

$$\text{at } x=2$$

$$\frac{dy}{dx} = \frac{3}{3x}$$

$$y = \ln(6)$$

$$\text{At } x=2.$$

$$\frac{dy}{dx} = \frac{3}{6}$$

$$m = \frac{1}{2}$$

$$\begin{aligned} \therefore y - \ln 6 &= \frac{1}{2}(x-2) \\ 2y - 2\ln 6 &= x-2 \\ &= x - 2y - 2 + 2\ln 6 \end{aligned}$$

$$\begin{aligned}
 \text{d) i. } & \int \sqrt{5x+1} \, dx \\
 & \int (5x+1)^{\frac{1}{2}} \, dx \\
 & = \frac{2(5x+1)^{\frac{3}{2}}}{3 \times 5} + C \\
 & = \frac{2(5x+1)^{\frac{3}{2}}}{15} + C
 \end{aligned}$$

$$\begin{aligned}
 \text{ii. } & \int \frac{x}{4+x^2} \, dx \\
 & = \frac{1}{2} \ln(4+x^2) + C
 \end{aligned}$$

$$\text{e) } \int_0^6 (x+k) \, dx = 30.$$

$$\left[\frac{x^2}{2} + kx \right]_0^6$$

$$\left(\frac{6^2}{2} + 6k \right) - (0 + (0)k) = 30$$

$$\therefore 18 + 6k = 30$$

$$6k = 12$$

$$k = 2.$$

Additional writing space on back page.