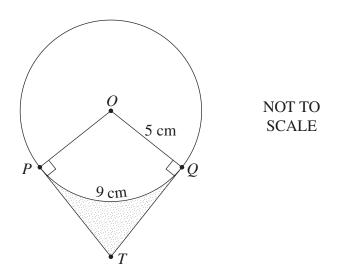
2010 HSC Mathematics

Question 6 (12 marks) Use the Question 6 Writing Booklet.

(a) Let $f(x) = (x+2)(x^2+4)$.

- (i) Show that the graph y = f(x) has no stationary points.
- (ii) Find the values of x for which the graph y = f(x) is concave down, and the values for which it is concave up.
- (iii) Sketch the graph y = f(x), indicating the values of the x and y intercepts.
- (b) The diagram shows a circle with centre O and radius 5 cm.

The length of the arc PQ is 9 cm. Lines drawn perpendicular to OP and OQ at P and Q respectively meet at T.



- (i) Find $\angle POQ$ in radians. 1
- (ii) Prove that $\triangle OPT$ is congruent to $\triangle OQT$.
- (iii) Find the length of *PT*.
- (iv) Find the area of the shaded region. 2