

Question 4.

a.  $3x^2 + 2x + k = 0$  has no real roots.

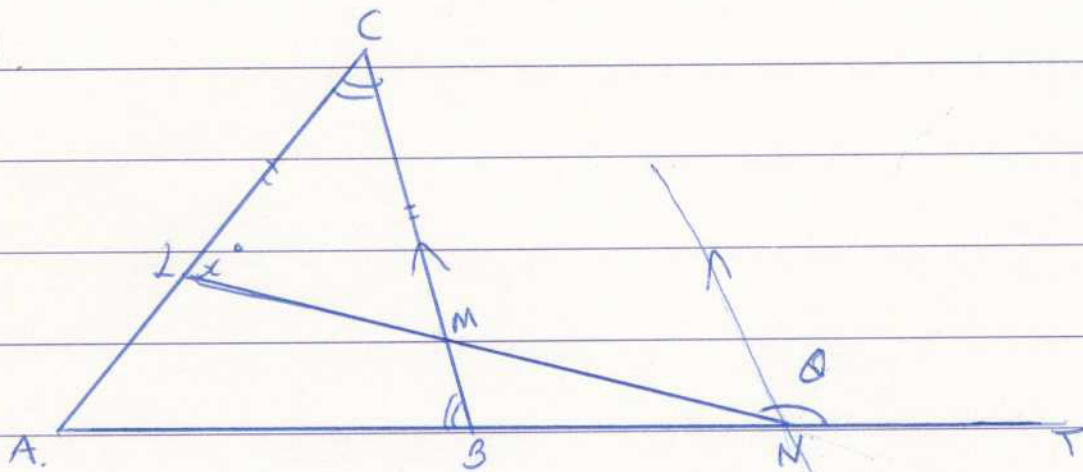
$$\Delta = b^2 - 4ac \leq 0$$

$$\therefore 4 - 12k < 0$$

$$12k > 4$$

$$k > \frac{1}{3}$$

b)



i). show  $\angle ABC = 180 - 2x^\circ$

~~proof~~

$\triangle CLM$  is isosceles  $\therefore$

$$\therefore \angle CLM = \angle CML = x^\circ$$

$\therefore$  both angles =  $2x$

then  $180$  (sum of a  $\Delta$ )  $- 2x = \angle LCM$

$$\angle LCM = \angle ABC$$

$$\therefore \angle ABC = 180 - 2x^\circ$$

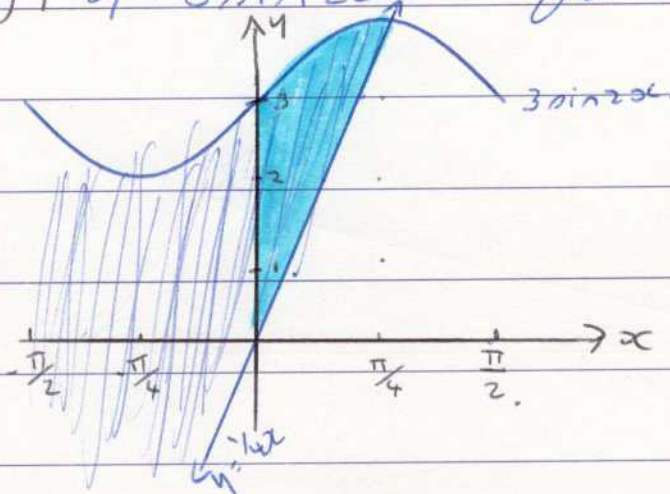
ii show that  $\angle TNL = 3x^\circ$

$x^\circ$  because of  $\parallel$ 's alternate angles.

$180 - y = 3x^\circ$  because of  $\parallel$ 's and alternate angles.

$$\angle TNL = 3x^\circ$$

c) i  $y = 3 \sin 2x$  for  $-\frac{\pi}{2} \leq x \leq \frac{\pi}{2}$ .



shaded region.

ii sketch  $y = \frac{1}{4}x$

$(0, 0), (1, \frac{1}{4}), (-1, -\frac{1}{4}), (2, \frac{1}{2}), (-2, -\frac{1}{2})$

$$\int_0^{\pi/4} (3 \sin 2x - \frac{1}{4}x) dx$$

$$= \left[ -\frac{3}{2} \cos 2x - \frac{1}{8}x^2 \right]_0^{\pi/4}$$

iii

$$\int_0^{\pi/4} (3 \sin 2x - \frac{1}{4}x) dx$$

$$= \left[ -\frac{3}{2} \cos 2x - \frac{1}{8}x^2 \right]_0^{\pi/4}$$

$$= \left( -\frac{3}{2} \times 0 - \frac{1}{8}x^2 \right) -$$

$$= \left( \frac{3}{2} - 0 \right)$$

$$= \frac{3}{2} - \frac{1}{8} - \frac{3}{2}$$



$$= -254 \frac{5}{8}$$